

NAME _____

FACTORIAL – IV (JS only)

PRINCIPLE

The **factorial** variation works in combination with other variations.

Factorial in Combination with Other Variations

- (a) # factors $x(5!) = x120 = x(2^3 \times 3^1 \times 5^1) = 4 \times 2 \times 2 = 16$.
- (b) Small. prime $x(6!)$ is not allowed since 6! is bigger than 200. However $x(5!) = x120 = 127$.
- (c) Red exp. A Goal of 23 (red 3) may be interpreted as $2^{3!}$ or 2^6 . In a Solution write $2^{(3!)}$ to prevent an opponent from interpreting the expression as $(2^3)!$
- (d) 0 or x wild 0 or x may not stand for ! because ! is not a symbol on the cubes.
- (e) Sr: $\sqrt{=} i$ $\sqrt{3!}$ must be written $\sqrt{(3!)}$ or $3!\sqrt{}$ to prevent an opponent from interpreting it as $(\sqrt{3})!$, which is undefined.

EXERCISES

Give each possible value of each expression. Assume factorial is in effect along with the variation listed.

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| <ul style="list-style-type: none"> 1. sideways $(6 \times \infty)!$ _____ 3. # factors $x3!$ _____ 5. smallest prime $x(4!)$ _____ 7. red exponent $33!$ _____ 9. base 8 $12! \div (10!)$ _____ 11. base 11 $(21 - 1x)!$ _____ 13. Sr: $\sqrt{=} i$ $5!\sqrt{}$ _____ | <ul style="list-style-type: none"> 2. upside-down $(4 - \infty)!$ _____ 4. # factors $x(4!)$ _____ 6. smallest prime $x3!$ _____ 8. average $3! + (5!)$ _____ 10. base 9 $11! \div [(5 + 4)!]$ _____ 12. base 12 $\sqrt{!} - (x!)$ _____ 14. Sr: log $(8 \cdot 2)!$ _____ |
|---|--|

15. Complete this table. x represents number of factors.

n	n!	x(n!)	n	n!	x(n!)
0	1	1	5		
1	1	1	6		
2	2	2	7		
3	6	4	8		
4			9		

16. If x represents **smallest prime**, what is the smallest value of n for which x(n!) is illegal? _____

Simplify each expression.

Sample $\sqrt{(6!)} = \sqrt{(6 \times 5 \times 4 \times 3 \times 2)} = \sqrt{[(6 \times 3 \times 2) \times 4 \times 5]} = 6 \times 2 \times \sqrt{5} = \frac{12 \times \sqrt{5}}{\text{Goal to set}}$

- | | |
|-------------------------|-------------------------|
| 17. $\sqrt{(5!)}$ _____ | 18. $\sqrt{(7!)}$ _____ |
| 19. $\sqrt{(8!)}$ _____ | 20. $\sqrt{(9!)}$ _____ |

MORE CHALLENGING EXERCISES

With **factorial** and **mult. op.**, use all the Resources listed to write a Solution for each Goal.

- | Goal | Resources | Solution | Goal | Resources | Solution |
|--------------------|-----------|----------|-----------------|---------------------|----------|
| 21. 80×54 | 6 7 - | _____ | 22. $1 \div 10$ | 6 7 9 $\div \times$ | _____ |
| 23. 24×34 | 4 5 6 - + | _____ | 24. 66 | 4 5 7 + \div | _____ |